STAT4101 Homework 7, due October 31, 2007

Chapter 4: 59, 63, 69a, 76, 77, 78, 81, 99, 101, 118, and ...

Prove this more general form of Tchebysheff's inequality,

$$P(X \ge a) \le \frac{E(X)}{a},$$

and show that the version in your book follows from it.

Hint: Start by writing out the expectation and splitting it into two parts, with the split on a. Then follow the same logic as in the proof in the book on page 195. To show that the version in the book follows, let $X = (Y - EY)^2$ and $a = t^2\sigma^2$, where $\sigma^2 = \text{Var}(Y)$.