

$$Q_n(\theta) = \sum_{i=1}^P t_i(x) g_i(\theta) - h(\theta) + u(x)$$

$$= \sum_{i=1}^P y_i \psi_i - h(\theta) + u(x)$$

$$f_\theta(x) = \exp\left(\sum_i y_i \psi_i - h(\theta) + u(x)\right)$$

$$1 = \int f_\theta(x) dx = e^{-h(\theta)} \int \exp\left(\sum_i y_i \psi_i + u(x)\right) dx$$

$$\frac{\partial}{\partial \psi_k} \left[\sum_{i=1}^p y_i \psi_i - C(\psi) \right]$$

$$= y_k - \frac{\partial C(\psi)}{\partial \psi_k}$$

$$\nabla \ell(\psi) = y - \nabla C(\psi)$$

$$E(y - \nabla C(\psi)) = 0$$

$$\parallel$$
$$E(y) - \nabla C(\psi)$$

so

$$E(y) = \nabla C(\psi)$$

$$\text{var}(y - \nabla C(\psi)) = -E\left(-\nabla^2 C(\psi)\right)$$

\parallel \parallel

$\text{var}(y)$ $\nabla^2 C(\psi)$

$$\sum_{i=1}^n \left[\sum_{j=1}^n t_i(x_j) g_i(\theta) - h(\theta) \right]$$

$$\sum_{i=1}^n g_i(\theta) \sum_{j=1}^n t_i(x_j) - nh(\theta)$$